

Towards Understanding the Geometry of Knowledge Graph Embeddings

Chandras

Indian Institute of Science
chandras@iisc.ac.in

Aditya Sharma

Indian Institute of Science
adityasharma@iisc.ac.in

Partha Talukdar

Indian Institute of Science
ppt@iisc.ac.in

<http://aclweb.org/anthology/P18-1012>

<http://anthology.aclweb.org/attachments/P/P18/P18-1012.Notes.pdf>

紹介者: 笹野遼平 (名大)

はじめに

- なぜこの論文を選んだか:
 - Embeddingの形状(geometry)分析に興味(how to?)
 - cf. SGNSの形状分析 [Mimno & Thompson ACL'17]
 - 最先端NLP勉強会@東京8/3,4で紹介されなかった
- 概要:
 - 6つの知識グラフ(Knowledge Graph)の埋め込み手法でそれぞれ得られた要素/形状ベクトルの形状を始めて分析
 - 主に中心ベクトルとの類似度(ATM)を分析
 - Additiveな手法とMultiplicativeな手法(後述)で大きな違い
 - 前者では0を中心に広く分散
 - 後者では正の値を偏り、分散は小さめ(SGNSと近い傾向)
 - パフォーマンス等の分析はかなり微妙な印象

形状分析の先行研究: The strange geometry of skip-gram with negative sampling [Mimno & Thompson'17]

Figure 2

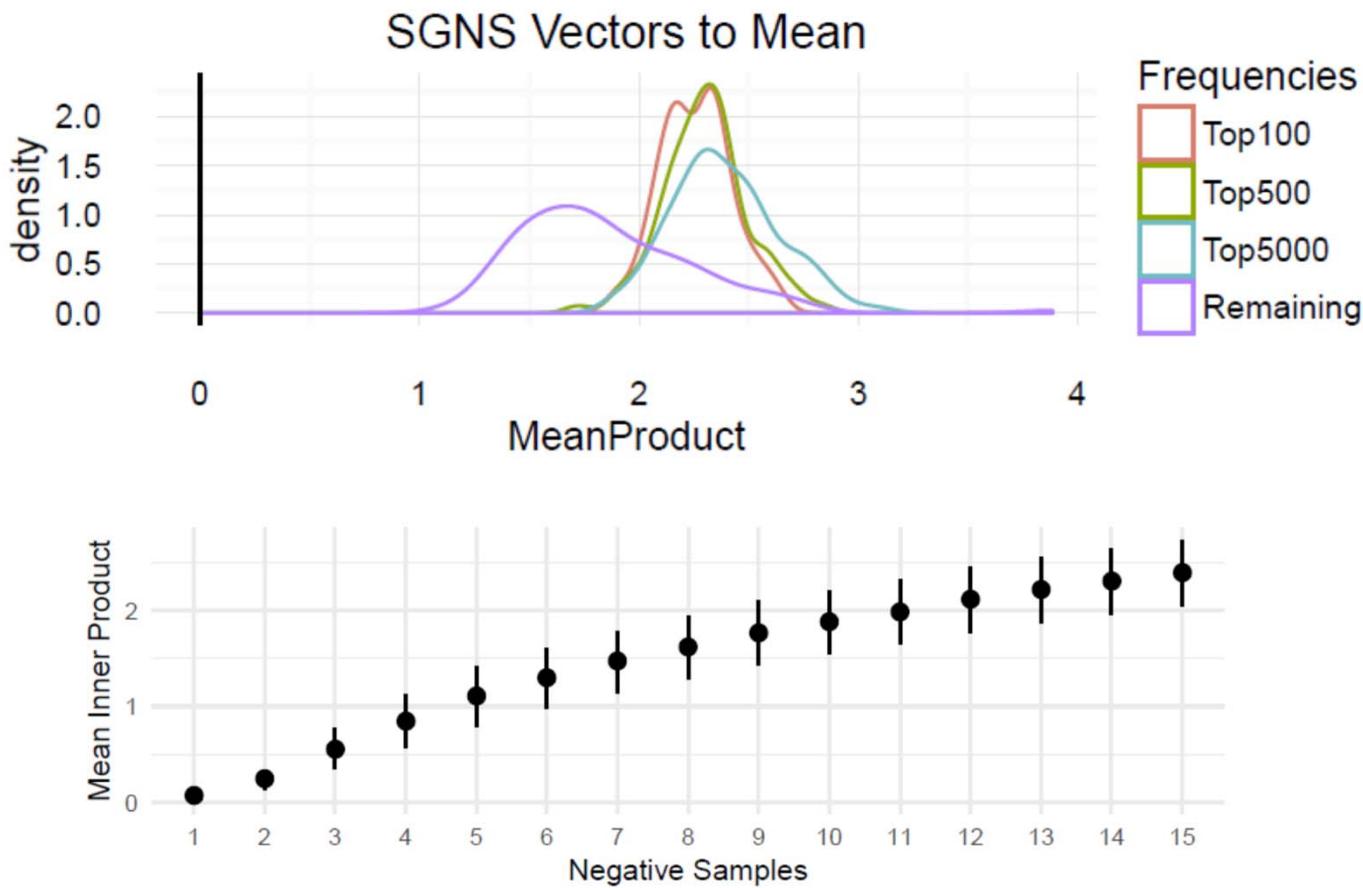
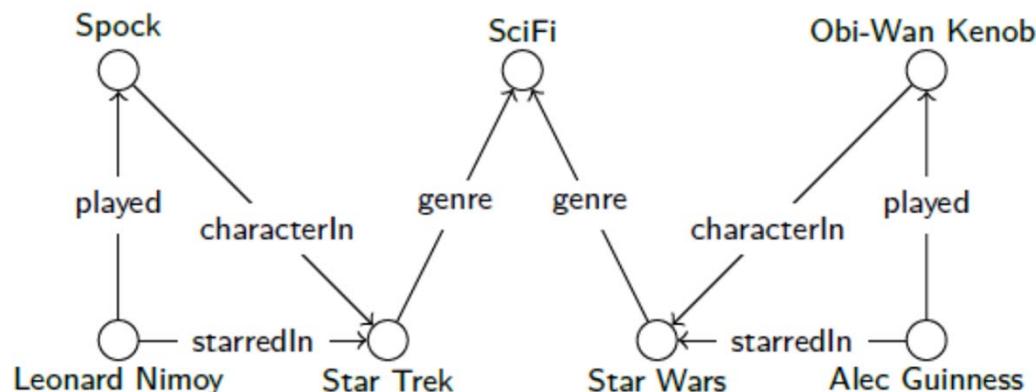


Figure 6: The number of negative samples affects the inner product between vectors and the mean vector. Results are indistinguishable across 10 initializations for each value.

知識グラフ(KG: knowledge graph)

- 有向グラフの形で表された知識(e.g. FreeBase)
 - それぞれのノードがエンティティ
 - ノード間にエッジを張り、関係をラベルで表現
 - $(h; r; t)$ の形(三つ組: triplet)で表現 (h :始点, r : 関係, t : 終点)
 - e.g. J. K. Rowling [influenced by] C. S. Lewis



Graph Embedding (グラフ埋め込み)

- 知識グラフをベクトル空間上に埋め込む手法
- 代表的な手法: TransE [Bordes+'13]
 - 知識ベースに含まれる三つ組(h ; r ; t) に対し、
 $h + r = t$ が成立するようにベクトルを学習
 - 他の三つ組に対しては成立しないようにしたい
⇒ negative sampling で負例を生成し学習
- 応用: Link Prediction, Entity Classification

分析対象のグラフ埋め込み手法

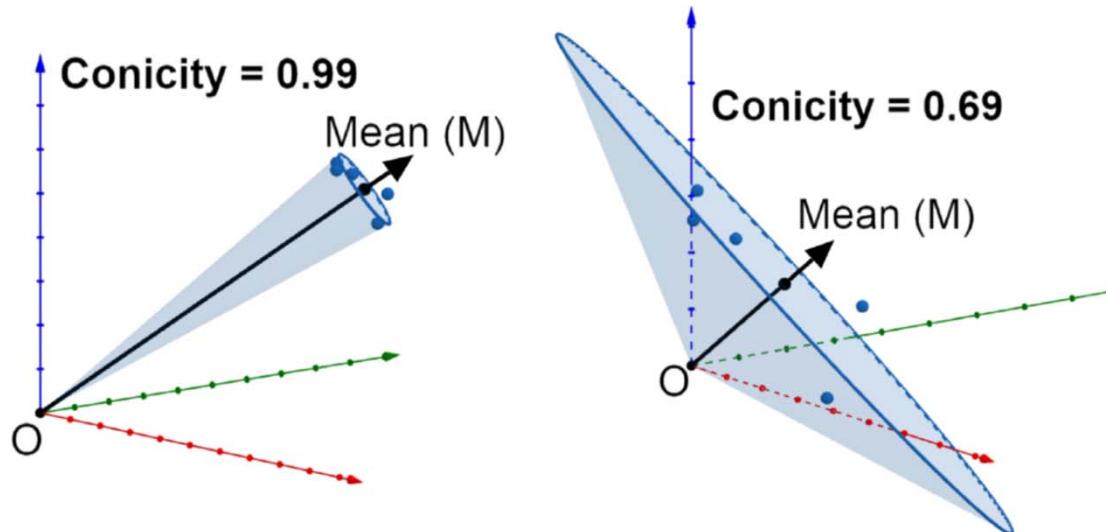
Type	Model	Score Function $\sigma(h, r, t)$
Additive	TransE (Bordes et al., 2013)	$-\ h + r - t\ _1$
	TransR (Lin et al., 2015)	$-\ M_r h + r - M_r t\ _1$
	STransE (Nguyen et al., 2016)	$-\ M_r^1 h + r - M_r^2 t\ _1$
Multiplicative	DistMult (Yang et al., 2014)	$r^\top (h \odot t)$
	HolE (Nickel et al., 2016)	$r^\top (h \star t)$
	ComplEx (Trouillon et al., 2016)	$\text{Re}(r^\top (h \odot \bar{t}))$

cf. 知識グラフの埋め込みとその応用[林克彦'17]

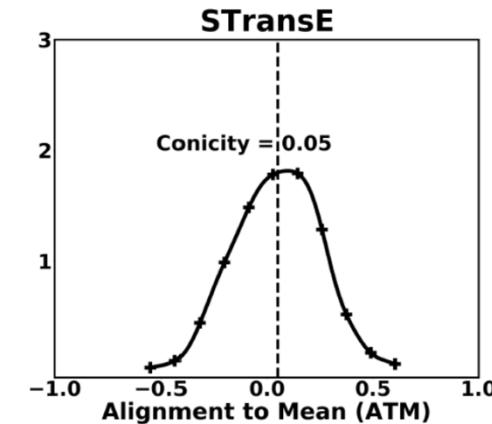
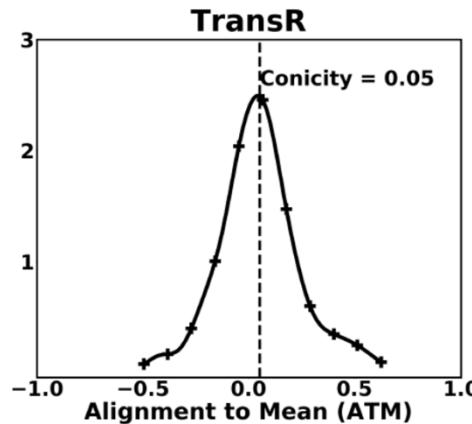
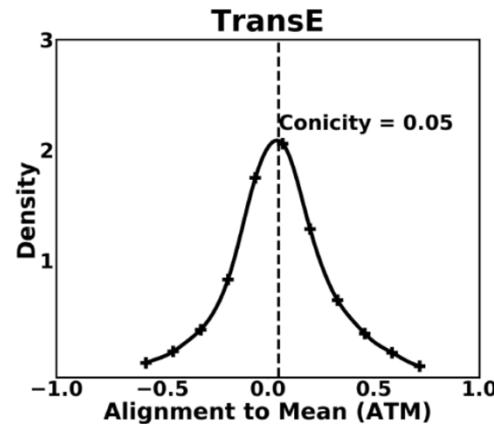
<http://www.kecl.ntt.co.jp/icl/lirg/members/hayashi/files/stairs-hayashi17.pdf>

ベクトルの分析指標

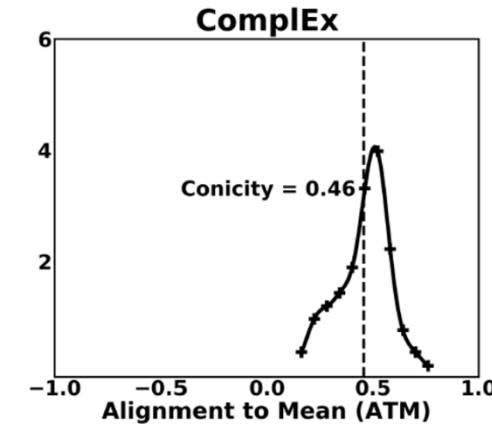
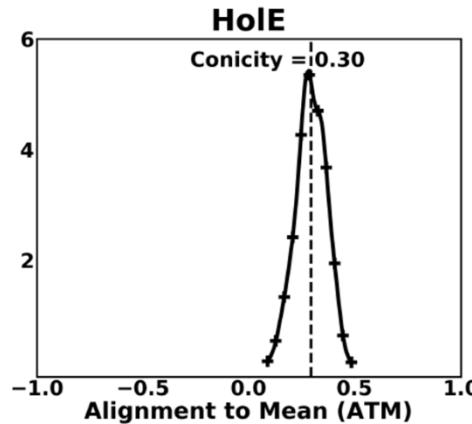
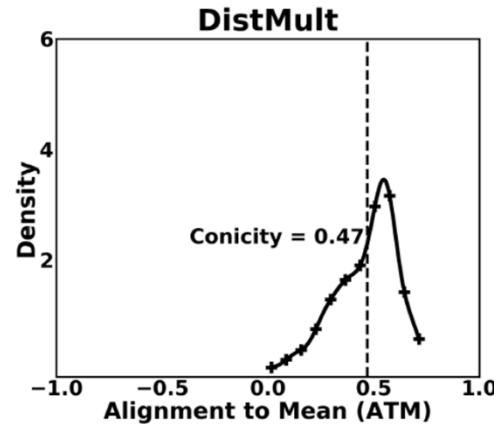
- 平均ベクトルとの類似度: $\text{ATM}(\mathbf{v}, \mathbf{V}) = \cosine\left(\mathbf{v}, \frac{1}{|\mathbf{V}|} \sum_{\mathbf{x} \in \mathbf{V}} \mathbf{x}\right)$
(alignment to mean)
- ATMの平均(円錐形度合): $\text{Conicity}(\mathbf{V}) = \frac{1}{|\mathbf{V}|} \sum_{\mathbf{v} \in \mathbf{V}} \text{ATM}(\mathbf{v}, \mathbf{V})$
- ATMの分散(vector spread): $\text{VS}(\mathbf{V}) = \frac{1}{|\mathbf{V}|} \sum_{\mathbf{v} \in \mathbf{V}} \left(\text{ATM}(\mathbf{v}, \mathbf{V}) - \text{Conicity}(\mathbf{V}) \right)^2$
- ベクトルの平均長: $\text{AVL}(\mathbf{V}) = \frac{1}{|\mathbf{V}|} \sum_{\mathbf{v} \in \mathbf{V}} \|\mathbf{v}\|_2$



手法ごとの要素ベクトルのATM

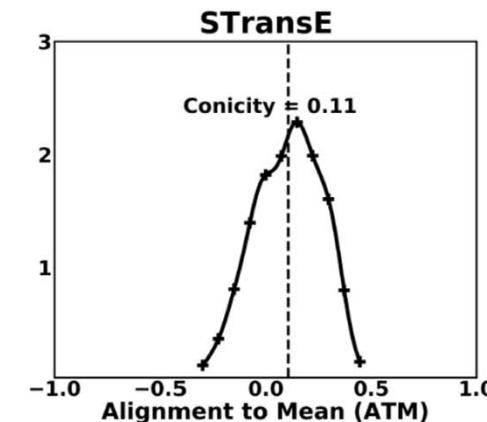
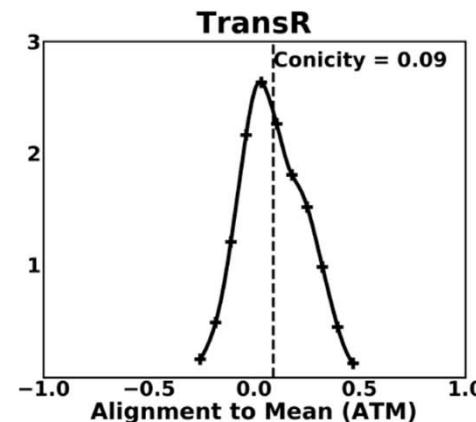
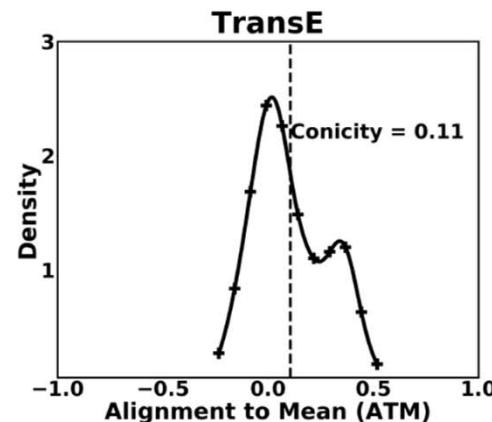


(a) Additive Models

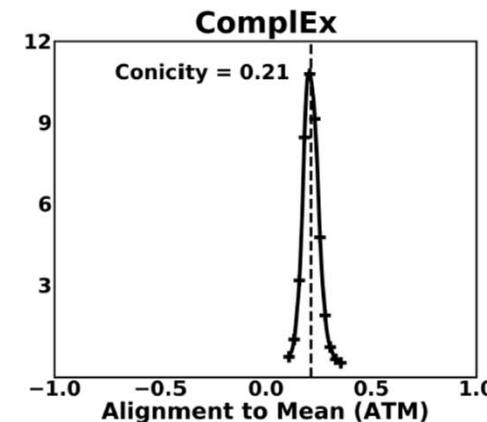
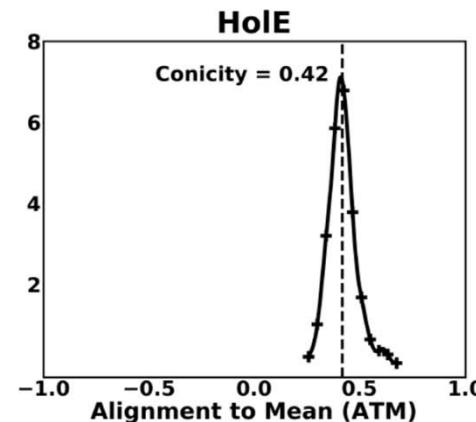
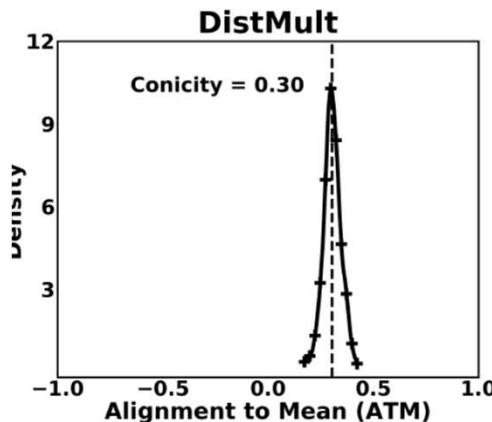


(b) Multiplicative Models

手法ごとの関係ベクトルのATM



(a) Additive Models



(b) Multiplicative Models

negative sampleの数の影響

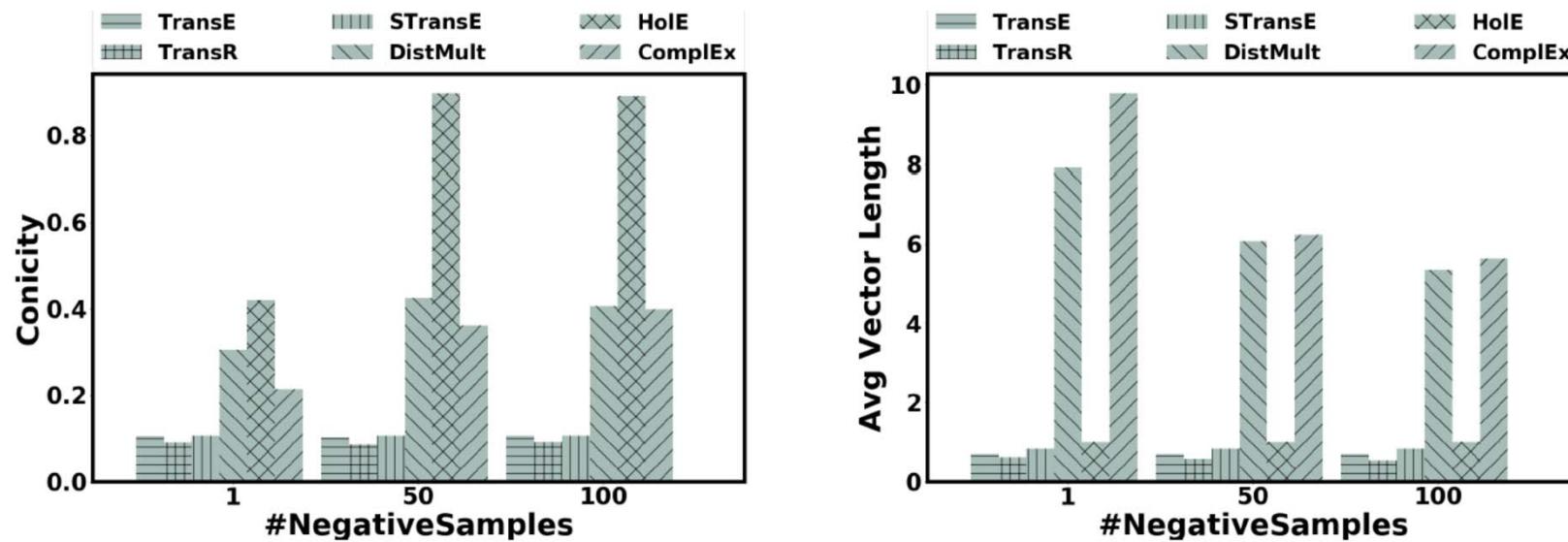


Figure 4: Conicity (left) and Average Vector Length (right) vs Number of negative samples for entity vectors learned using various KG embedding methods. In each bar group, first three models are additive, while the last three are multiplicative. Main findings from these plots are summarized in Section 6.2

ベクトルの次元数の影響

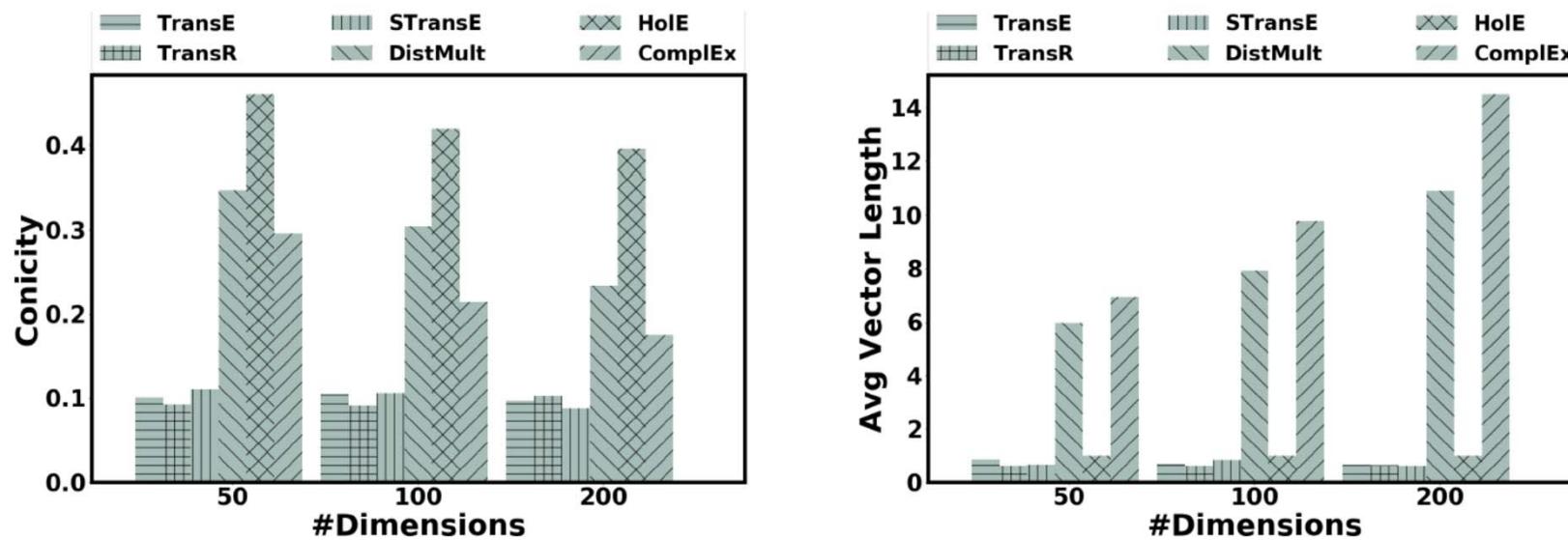


Figure 5: Conicity (left) and Average Vector Length (right) vs Number of Dimensions for entity vectors learned using various KG embedding methods. In each bar group, first three models are additive, while the last three are multiplicative. Main findings from these plots are summarized in Section 6.3.

パフォーマンスとの関係

- In Figure 6 (right), for all multiplicative models except HolE, a higher average entity vector length translates to better performance, while the number of negative samples is kept fixed

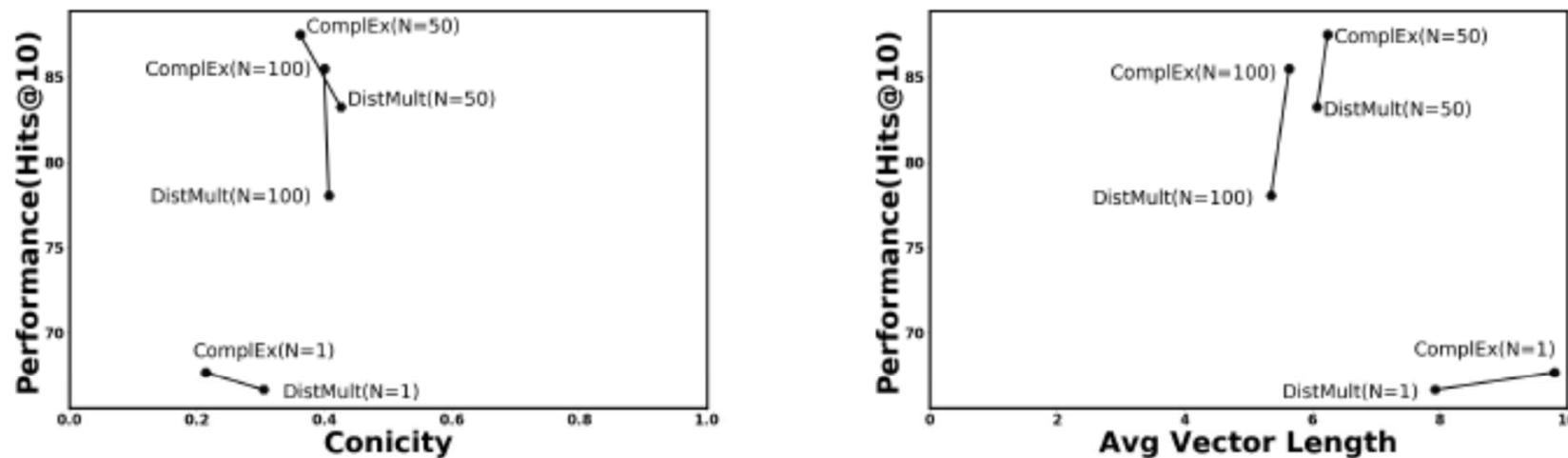


Figure 3: Relationship between Performance (HITS@10) on a link prediction task vs Conicity (left) and Avg. Vector Length (right) on FB15k dataset. For each point, N represents the number of negative samples used. Models with same number of negative samples are connected by line segment. This demonstrates that model performance has negative correlation with Conicity while positive correlation with average vector length for fixed number of negatives. Main findings are summarized in Section 3.